uc3m Universidad Carlos III de Madrid

COURSE: CALCULUS II

DEGREE: BACHELOR IN INDUSTRIAL TECHNOLOGIES ENGINEERING ACADEMIC YEAR: 2021-2022 TERM: 2

28 sessions along 14 weeks

WEEKLY PLANNING							
WEEK	SES	DESCRIPTION	GROUPS (mark X)		WEEKLY PROGRAMMING FOR STUDENT		
VVEER	N	DESCRIPTION		SEMINARS	DESCRIPTION	CLASS HOURS	HOMEWORK HOURS (Max. 7h week)
1	1	CHAPTER 1: DIFFERENTIAL CALCULUS IN SEVERAL VARIABLES 1.1 R ⁿ as an Euclidean space; topology 1.2 Functions of n variables - Functions, graphs, and level sets	Х		Sections 14.1 and 16.2 [WHT] and/or sections 1.5, 2.1, 2.2 [MT]	1,67	6,3
1	2	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
2	3	1.3 Limits and Continuity	Х		Section 14.2 [WHT] and/or section 2.2 [MT]	1,67	6,3
2	4	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	0,3
3	5	1.4 DifferentiabilityPartial derivativesDerivative; Jacobian matrix	Х		Section 14.3 [WHT] and/or section 2.3 [MT]	1,67	6,3
3	6	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
4	7	Properties of the derivativeChain ruleDirectional derivatives; gradient vector	х		Sections 14.3-14.6 [WHT] and/or sections 2.5, 2.6 [MT]	1,67	6,3
4	8	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
5	9	CHAPTER 2: LOCAL PROPERTIES OF FUNCTIONS 2.1 Higher order derivatives - Iterated derivatives; equality of mixed partials - Differential operators: divergence, curl, Laplacian	Х		Sections 16.4, 16.7, 16.8 [WHT] and/or sections 3.1, 3.2 [MT]	1,67	6,3
5	10	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
6	11	- Taylor polynomial; Hessian matrix	Х		Sections 14.7, 14.9 [WHT] and/or sections	1,67	6,3

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		2.2 Optimization			3.2, 3.3 [MT]		
		- Local extrema					
		- Absolute/global extrema					
6	12	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
7	13	Free optimization problemsConstrained optimization: Lagrange multipliers	Х		Sections 14.7, 14.9 [WHT] and/or section 3.3, 3.4 [MT]	1,67	6,3
7	14	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
	15	CHAPTER 3: INTEGRAL CALCULUS ON R ⁿ	Х		Sections 15.1, 15.5 [WHT] and/or sections	1,67	
		3.1 Double and triple integrals			5.1-5.2 [MT]		
8		- Iterated integrals					
		- Cavalieri's principle					6,3
		- Integrals over rectangular regions; Fubini's theorem					
8	16	First partial exam		Х	(**) Problem solving for selected exercises	1,67	
		(*) Discussion of selected exercises				_,	
	17	- Arbitrary 2- and 3-dimensional regions	V		Sections 15.2, 15.3, 15.5 [WHT and/or	4 / 7	
9	1/	- Change in the order of integration 3.2 n-dimensional integrals	Х		sections 5.3-5.5 [MT]	1,67	6,3
9	18	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
	10	3.3 Changes of variables and applications			Sections 15.4, 15.6-15.8 [SHE] and/or sections	1,07	
		- Changes of variables; Jacobian			6.1-6.3 [MT]		
10	19	- Polar, cylindrical, and spherical coordinates	Χ			1,67	6,3
		- Average; center of mass; moments of inertia					5,0
10	20	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
	21	CHAPTER 4: INTEGRALS OVER CURVES AND SURFACES	Х		Sections 16.1-16.3 [WHT] and/or sections 7.1,	1,67	
		4.1 Line integrals			7.2 [MT]		
11		- Parametrized curves					
		- Line integral					6,3
		- Conservative fields					ŕ
11	22	(*) Discussion of selected exercises		V	(**) Problem solving for selected exercises	4 / 7	
11	22			Х		1,67	
		4.2 Surface integrals			Sections 16.5, 16.6 [WHT] and/or sections		
12	23	- Parametrized surfaces	Х		7.3-7.6 [MT]	1,67	
12	۷3	- Area of a Surface	٨			1,07	6,3
		- Integrals of scalar functions and vector fields					
12	24	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	

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		- Conservative fields			Sections 16.7, 16.8 [WHT] and/or sections			
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13	26	(*) Discussion of selected exercises		X	, , , , , , , , , , , , , , , , , , , ,	1,67		
40		Second partial exam			(**) Problem solving for selected exercises	4.77	,	
	23	- Stokes' theorem	^		0.1, 0.2 []	1,07	6,3	
13	25	4.3 Integral theorems of vector analysisPlanar case: Green's and divergence theorems	v		Sections 16.4, 16.7 [WHT] and/or sections 8.1, 8.2 [MT]	1,67		

Total 1 (Hours of class plus student homework hours between weeks 1-14)	135

Total 2 (Hours of class plus student homework hours between weeks 15-18)					15			
Subtotal 2						3	12	
18								
17		Assessment, final exam preparation				3	10	
16								
15		Tutorials, handing-in, etc.					2	

TOTAL (Total 1 + Total 2. <u>Maximum 180 hours</u>) 150

Notes:

[MT] Marsden and Tromba, "Vector Calculus", W. H. Freeman (6th edition, 2012) [WHT] Weir, Hass and Thomas, "Thomas' Calculus", Wiley (12th edition, 2009)

- (*) Discussion of selected exercises from the course collection that correspond to the previous lecture
- (**) Problem solving for selected exercises from the course collection and sections of [MT], [WHT] that correspond to the previous lecture
- (+) Lecture hours are always 1.67 (1.67 hours*28 sessions = 46.76 hours)