

**COURSE: CALCULUS II**

**DEGREE: Bachelor in Data Science and Engineering and Telecommunication Technologies Engineering**

**ACADEMIC YEAR: 2024-2025**

**TERM: 2**

**28 sessions along 14 weeks**

WEEKLY PLANNING							
WEEK	SESSION	DESCRIPTION	GROUPS (mark X)		WEEKLY PROGRAMMING FOR STUDENT		
			LECTURES	SEMINARS	DESCRIPTION	CLASS HOURS	HOMEWORK HOURS (Max. 7h week)
1	1	<b>CHAPTER 1: DIFFERENTIAL CALCULUS IN SEVERAL VARIABLES</b> 1.1 $\mathbb{R}^n$ as an Euclidean space; topology 1.2 Functions of n variables - Functions, graphs, and level sets	X		Sections 1.5, 2.1, 2.2 [MT]	1,67	6,3
1	2	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
2	3	1.3 Limits and Continuity	X		Section 2.2 [MT]	1,67	6,3
2	4	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
3	5	1.4 Differentiability - Partial derivatives - Derivative; Jacobian matrix	X		Section 2.3 [MT]	1,67	6,3
3	6	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
4	7	- Properties of the derivative - Chain rule - Directional derivatives; gradient vector	X		Sections 2.5, 2.6 [MT]	1,67	6,3
4	8	(*) Discussion of selected exercises		X	(**) Problem solving for selected	1,67	

					exercises		
5	9	<b>CHAPTER 2: LOCAL PROPERTIES OF FUNCTIONS</b> 2.1 Higher order derivatives <ul style="list-style-type: none"> <li>- Iterated derivatives; equality of mixed partials</li> <li>- Differential operators: divergence, curl, Laplacian</li> </ul>	X		Sections 3.1, 3.2 [MT]	1,67	6,3
5	10	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
6	11	- Taylor polynomial; Hessian matrix 2.2 Optimization <ul style="list-style-type: none"> <li>- Local extrema</li> <li>- Absolute/global extrema</li> </ul>	X		Sections 3.2, 3.3 [MT]	1,67	6,3
6	12	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
7	13	<ul style="list-style-type: none"> <li>- Free optimization problems</li> <li>- Constrained optimization: Lagrange multipliers</li> </ul>	X		Section 3.3, 3.4 [MT]	1,67	6,3
7	14	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
8	15	<b>CHAPTER 3: INTEGRAL CALCULUS ON <math>\mathbb{R}^n</math></b> 3.1 Double and triple integrals <ul style="list-style-type: none"> <li>- Iterated integrals</li> <li>- Cavalieri's principle</li> <li>- Integrals over rectangular regions; Fubini's theorem</li> </ul>	X		Sections 5.1-5.2 [MT]	1,67	6,3
8	16	<b>First partial exam</b> (*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
9	17	<ul style="list-style-type: none"> <li>- Arbitrary 2- and 3-dimensional regions</li> <li>- Change in the order of integration</li> </ul> 3.2 n-dimensional integrals	X		Sections 5.3-5.5 [MT]	1,67	6,3

9	18	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
10	19	3.3 Changes of variables and applications <ul style="list-style-type: none"> <li>- Changes of variables; Jacobian</li> <li>- Polar, cylindrical, and spherical coordinates</li> <li>- Average; center of mass; moments of inertia</li> </ul>	X		Sections 6.1-6.3 [MT]	1,67	6,3
10	20	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
11	21	<b>CHAPTER 4: INTEGRALS OVER CURVES AND SURFACES</b> 4.1 Line integrals <ul style="list-style-type: none"> <li>- Parametrized curves</li> <li>- Line integral</li> <li>- Conservative fields</li> </ul>	X		Sections 7.1, 7.2 [MT]	1,67	6,3
11	22	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
12	23	4.2 Surface integrals <ul style="list-style-type: none"> <li>- Parametrized surfaces</li> <li>- Area of a Surface</li> <li>- Integrals of scalar functions and vector fields</li> </ul>	X		Sections 7.3-7.6 [MT]	1,67	6,3
12	24	<b>Second partial exam</b> (*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
13	25	4.3 Integral theorems of vector analysis <ul style="list-style-type: none"> <li>- Planar case: Green's and divergence theorems</li> <li>- Stokes' theorem</li> </ul>	X		Sections 8.1, 8.2 [MT]	1,67	6,3
13	26	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	
14	27	- Conservative fields	X		Sections 8.3, 8.4 [MT]	1,67	6,3

		- Gauss' theorem						
14	28	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67	6,3	
Subtotal 1							47	88
Total 1 (Hours of class plus student homework hours between weeks 1-14)							135	
15		Tutorials, handing-in, etc.				2		
16		Assessment, final exam preparation				3	10	
17								
18								
Subtotal 2							3	12
Total 2 (Hours of class plus student homework hours between weeks 15-18)							15	
TOTAL (Total 1 + Total 2. <u>Maximum 180 hours</u> )							150	

**Notes:**

[MT] Marsden and Tromba, "Vector Calculus", W. H. Freeman (6<sup>th</sup> edition, 2012)

(\*) Discussion of selected exercises from the course collection that correspond to the previous lecture

(\*\*) Problem solving for selected exercises from the course collection and sections of [MT] that correspond to the previous lecture

(+) Lecture hours are always 1.67 (1.67 hours\*28 sessions = 46.76 hours)