Universidad
Carlos III de Madrid
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## COURSE: LINEAR ALGEBRA

| DEGREE: Aerospace Engineering | YEAR: 1 | TERM: 1 |
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| $\begin{aligned} & \sum_{\text {N }}^{\text {n }} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { SESSION } \\ & 45,46 \& 47 \end{aligned}$ | DESCRIPTION | GROUP |  | WEEKLY PROGRAMMING FOR STUDENTS |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | LECTURE | SEMINAR | NOTES | LECTURE HOURS | STUDENT WORK |
| 1 | 15/9 | 0. Complex Numbers <br> 0.1 First operations <br> - Definition. Binomial form <br> - Sum and product <br> - Graphical representation <br> 0.2 Further operations <br> - Conjugate, modulus and argument <br> - Division | X |  | Book study, Appendix A [N] | 1,66 | 6 |
| 1 | 16/9, \& 18/9 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 2 | 22/9 | 0.2 Exponential form <br> - Exponential form <br> - Roots of a complex number | X |  | Book study, Appendix A [N] | 1,66 | 6 |
| 2 | 23/9, \& 25/9 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 3 | 29/9 | 1. Systems of linear equations <br> 1.1 Solving linear equations <br> - Matrix notation <br> - Gaussian elimination <br> 1.2 Row reduction and echelon forms <br> - Uniqueness <br> - Solutions of linear systems | X |  | Book study, chapters 1.1-1.2 [L] | 1,66 | 6 |
| 3 | 30/9 \& 2/10 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 4 | 6/10 | 1.3 Vector equations <br> - Vectors and linear combinations <br> - Subset spanned by vectors <br> 1.4 The matrix equation $A x=b$ <br> - Matrix times vector <br> - Solutions of a SLE | X |  | Book study, chapters 1.3-1.5 [L] | 1,66 | 6 |
| 4 | 7/10 \& 9/10 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |


| 5 | 13/10 | 2. Matrices <br> 2.1 Matrix Operations <br> - Sum and product by scalars <br> - Product <br> - Transpose of a matrix <br> 2.2 Inverse of a matrix <br> - Relation with the uniqueness of $A x=b$ <br> - Computation | X |  | Book study, chapters 2.1-2.3 [L] | 1,66 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 14/10 \& 16/10 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 6 | 20/10 | 3. Vector spaces <br> 3.1 Vector Spaces and Subspaces <br> - Sub-spaced generated by vectors <br> - Null Space and Columns space | X |  | Book study, chapters 2.8, 4.1-4.2 de [L] | 1,66 |  |
| 6 | 21/10, \& 23/10 | Midterm test on chapters 0,1 and 2 <br> Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 | 6 |
| 7 | 27/10 | 3.2 Linear Independence and basis <br> - The spanning set theorem <br> - Basis for $\operatorname{Nul}(\mathrm{A})$ and $\operatorname{Col}(\mathrm{A})$ | X |  | Book study, chapters 1.7, 2.9, 4.3 [L] | 1,66 |  |
| 7 | 28/10 \& 30/10 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 8 | 3/11 | 3.3 Coordinate Systems <br> 3.4 The dimension of a vector space <br> - The basis theorem <br> - The dimensions of $\operatorname{Nul}(\mathrm{A})$ and $\operatorname{Col}(\mathrm{A})$ <br> 3.5 Rank <br> - The Rank theorem <br> - 3.6 Change of basis | X |  | Book study, chapters 4.4-4.5 [L] and 2.9, 4.6-4.7 [L] | 1,66 | 6 |
| 8 | 4/11 \& 6/11 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 9 | 10/11 | 3.7 Linear transformations <br> - The matrix of a linear transformation <br> - Kernel and range of a linear transformation | X |  | Book study, chapters 1.8-1.9 [L] | 1,66 | 6 |
| 9 | 11/11 \& 13/11 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 10 | 17/11 | 4. Eigenvalues and eigenvectors <br> 4.1 Definitions <br> - Revisiting determinants <br> - Linear Independence of eigenvalues <br> - Eigenspaces <br> 4.2 The characteristic equation | X |  | Book study, chapters 3.1 -3.2, 5.1-5.2 [L] | 1,66 | 6 |
| 10 | 18/11 \& 20/11 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |


| 11 | 24/11 | 4.3 Diagonalization <br> - The diagonalization theorem <br> - Diagonalizating matrices | X |  | Book study, chapter 5-3 [L] | 1,66 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 25/11 \& 27/11 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 12 | 1/12 | 5. Orthogonality <br> 5.1 Inner product, length and orthogonality <br> 5.2 Orthogonal sets <br> - Orthogonal and orthonormal basis <br> - Orthogonal matrices | X |  | Book study, chapters 6.1-6.2 [L] | 1,66 | 6 |
| 12 | 2/12 \& 4/12 | Midterm test on chapters 3 and 4 Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 13 | 4/12 | 5.3 Orthogonal projection <br> - The best approximation theorem <br> 5.4 The Gram-Schmidt process | X |  | Book study, chapters 6.3-6.4 [L] | 1,66 | 6 |
| 13 | 9/12 \& 11/12 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 |  |
| 14 | 15/12 | 5.5 Least square problems <br> - Normal equations <br> 6. Diagonalization of symmetric matrices <br> - Spectral theorem | X |  | Book study, chapter 6.5 [L] and | 1,66 | 6 |
| 14 | 16/12 \& 18/12 | Selected exercises (*) |  | X | Additional exercises from collection and textbooks (*) | 1,66 | 6 |
|  |  |  |  |  | Subtotal 1 | 50 |  |
|  |  |  | Total 1 (Hours of class plus student homework hours between weeks 1-15) |  |  | 140 |  |
|  | 16-18 | Assessment, evaluation preparation. Final Test |  |  |  | 3 | 7 |
|  |  |  |  |  | Subtotal 2 | 3 | 7 |
|  |  |  | Total 2 (Hours of class plus student homework hours between weeks 16-18) |  |  |  | 10 |
| TOTAL (Total 1 + Total 2 ) |  |  |  |  |  |  | 150 |

${ }^{(*)}$ ) Discussion of selected exercises from the course collection and from the recommended textbooks (W.K. Nicholson's ([N]) or D. C. Lay's ([L])) related with the theory session of the week. Compare with the solutions in the book

