## Universidad Carlos III de Madrid

Vicerrectorado de Estudios
Apoyo a la docencia y gestión del grado

## COURSE: Complex Variables and Transforms

DEGREE: Physical Engineering
YEAR: 2
TERM: 1

| WEEKLY PLANNING |  |  |  |  |  |  |  |  |  |
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| $\begin{gathered} \text { w } \\ \text { E } \\ \text { E } \\ \text { K } \end{gathered}$ | $\begin{aligned} & \text { S } \\ & \text { E } \\ & \text { S } \\ & \text { S } \\ & \text { I } \\ & \text { O } \end{aligned}$ | DESCRIPTION | TEACHING <br> (mark X) |  | SPECIAL ROOM <br> FOR SESSION <br> (Computer class room, audio-visual class room) | WEEKLY PROGRAMMING FOR STUDENT |  |  |  |
|  |  |  | L E $C$ $T$ U R E S | $\begin{gathered} \mathrm{S} \\ \mathrm{E} \\ \mathrm{M} \\ \mathrm{I} \\ \mathrm{~N} \\ \mathrm{~A} \\ \mathrm{R} \\ \mathrm{~S} \\ \hline \end{gathered}$ |  |  | DESCRIPTION | CLASS HOURS $(1,66=50+50$ <br> $\min )$ | HOMEWORK HOURS <br> (Max.Estim. 6,5h) |
| 1 | 1 | Complex numbers. Complex functions. Limits. Continuous functions. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 2 | Derivatives and Cauchy-Riemann equations. Harmonic functions. | XX |  |  | Exercises |  | 1,66 |  |
| 2 | 3 | Elementary functions. Polynomials. Exponential function. Trigonometric functions. Hyperbolic functions. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 4 | Logarithm. Complex exponents. Inverses of trigonometric and hyperbolic functions. | XX |  |  | Exercises |  | 1,66 |  |
| 3 | 5 | Integrals in the complex plane. Contour integrals. Cauchy-Goursat theorem. Cauchy formula. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 6 | Morera's theorem. Entire functions. Bounds for analytic functions. Fundamental theorem of algebra. | XX |  |  | Exercises |  | 1,66 |  |
| 4 | 7 | Sequences and convergence criteria. Power series. Radius of convergence. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 8 | Taylor series. Laurent series. Analytic continuation. | XX |  |  | Exercises |  | 1,66 |  |
| 5 | 9 | Power expansions and linear differential equations. Frobenius theory. |  |  |  | Exercises |  | 1,66 | 6,5 |
|  | 10 | Special functions of Mathematical Physics | XX |  |  | Exercises |  | 1,66 |  |


| WEEKLY PLANNING |  |  |  |  |  |  |  |  |  |
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| $\begin{gathered} \text { W } \\ \text { E } \\ \text { E } \\ \text { K } \end{gathered}$ | $\begin{aligned} & \text { S } \\ & \text { E } \\ & \text { S } \\ & \text { S } \\ & \text { I } \\ & \text { O } \end{aligned}$ | DESCRIPTION | TEACHING <br> (mark X) |  | SPECIAL ROOM <br> FOR SESSION <br> (Computer class room, audio-visual class room) | WEEKLY PROGRAMMING FOR STUDENT |  |  |  |
|  |  |  | L E C T U R E S | $\begin{gathered} \mathrm{S} \\ \mathrm{E} \\ \mathrm{M} \\ \mathrm{I} \\ \mathrm{~N} \\ \mathrm{~A} \\ \mathrm{R} \\ \mathrm{~S} \\ \hline \end{gathered}$ |  |  | DESCRIPTION | CLASS HOURS $(1,66=50+50$ $\min )$ | HOMEWORK HOURS (Max.Estim. $6,5 \mathrm{~h}$ ) |
| 6 | 11 | Zeros of a function. Singularities. Poles | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 12 | Residue formula. Residue theorem. Real integrals of trigonometric functions. | XX |  |  | Exercises |  | 1,66 |  |
| 7 | 13 | Real improper integrals. Integrals of functions with branch points. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 14 | Aplications of the residue Theorem to series summation | XX |  |  | Exercises |  | 1,66 |  |
| 8 | 15 | Summary of complex variables | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 16 | First partial test |  |  |  |  |  | 1,66 |  |
| 9 | 17 | Fourier series Basic definitions. The space of square integrable functions. Pointwise convergence. Uniform convergence. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 18 | Application of Fourier series to differential and partial differential equations. | XX |  |  | Exercises |  | 1,66 |  |
| 10 | 19 | Fourier transform. Basic definitions and properties. Inverse Fourier transform. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 20 | Convolution. Representation of aperiodic signals. Discrete time Fourier transform. | XX |  |  | Exercises |  | 1,66 |  |
| 11 | 21 | Laplace transform Definition, properties and convergence. Inverse Laplace transform. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 22 | Derivatives, integrals, and convolution. Applications to systems of linear differential equations. Transfer function. | XX |  |  | Exercises |  | 1,66 |  |
| 12 | 23 | z-transform. Convergence region and other properties. Inverse ztransform. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 24 | Transforms between continuous and discrete time signals. Applications to linear difference equations | XX |  |  | Exercises |  | 1,66 |  |
| 13 | 25 | Linear time-invariant (LTI) systems. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 26 | Analysis of LTI systems with transforms. | XX |  |  | Exercises |  | 1,66 |  |
| 14 | 27 | Summary of integral transforms. | XX |  |  | Exercises |  | 1,66 | 6,5 |
|  | 28 | Second partial test |  |  |  |  |  | 1,66 |  |




