Universidad
Carlos III de Madrid
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## COURSE: LINEAR ALGEBRA

DEGREE: Biomedical Engineering
YEAR: 1

| $\sum_{\text {而 }}^{<}$ | SESSION | DESCRIPTION | GROUP |  | WEEKLY PROGRAMMING FOR STUDENTS |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | LECTURE | SEMINAR | NOTES | LECTURE HOURS | STUDENT WORK |
| 1 | 1 | 1. Complex Numbers <br> 1.1 First operations <br> - Definition. Binomial form <br> - Sum and product <br> - Graphical representation <br> 1.2 Further operations <br> - Conjugate, modulus and argument <br> - Division |  | X | Book study, Appendix A [N] | 1,66 | 6 |
| 2 | 2 | 1.2 Exponential form <br> - Euler's formula <br> - Roots of a complex number | X |  | Book study, Appendix A [N] | 1,66 | 6 |
| 2 | 3 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 3 | 4 | 2. Sistems of linear equations <br> 2.1 Solving linear equations <br> - Matrix notation <br> - Gaussian elimination <br> 2.2 Row reduction and echelon forms <br> - Uniqueness <br> - Solutions of linear systems |  | X | Book study, chapters 1.1-1.2 [L] | 1,66 | 6 |
| 3 | 5 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 4 | 6 | 2.3 Vector equations <br> - Vectors and linear combinations <br> - Subset spanned by vectors <br> 2.4 The matrix equation $A x=b$ <br> - Matrix times vector <br> - Solutions of a SLE | X |  | Book study, chapters 1.3-1.5 [L] | 1,66 | 6 |
| 4 | 7 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |


| 5 | 8 | 3. Matrices <br> 3.1 Matrix Operations <br> - Sum and product by scalars <br> - Product <br> - Transpose of a matrix <br> 3.2 Inverse of a matrix <br> - Relation with the uniqueness of $A x=b$ <br> - Computation | X |  | Book study, chapters 2.1-2.3 [L] | 1,66 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 9 | Midterm test on chapters 1 and 2 Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 6 | 10 | 4. Vector spaces <br> 4.1 Vector Spaces and Subspaces <br> - Subspaced generated by vectors <br> - Null Sapce and Column space | X |  | Book study, chapters 2.8, 4.1-4.2 de [L] | 1,66 |  |
| 6 | 11 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 | 6 |
| 7 | 12 | 4.2 Linear Independence and bases <br> - The spanning set theorem <br> - Basis for $\operatorname{Nul}(\mathrm{A})$ and $\operatorname{Col}(\mathrm{A})$ | X |  | Book study, chapters 1.7, 2.9, 4.3 [L] | 1,66 |  |
| 7 | 13 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 8 | 14 | 4.3 Coordinate Systems <br> 4.4 The dimension of a vector space <br> - The basis theorem <br> - The dimensions of $\operatorname{Nul}(\mathrm{A})$ and $\operatorname{Col}(\mathrm{A})$ | X |  | Book study, chapters 4.4-4.5 [L] | 1,66 | 6 |
| 8 | 15 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 9 | 16 | 4.5 Rank <br> - The Rank theorem <br> 4.6 Change of basis |  |  | Book study, chapters 2.9, 4.6-4.7 [L] |  |  |
| 9 | 17 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 10 | 18 | 4.7 Linear transformations <br> - The matrix of a linear transformation <br> - Kernel and range of a linear transformation | X |  | Book study, chapters 1.8-1.9 [L] | 1,66 | 6 |
| 10 | 19 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 11 | 20 | 5. Eigenvalues and eigenvectors <br> 5.1 Definitions <br> - Revisiting determinants <br> - Linear Independence of eigenvectores <br> - Eigenspaces <br> 5.2 The characteristic equation | X |  | Book study, chapters 3.1 -3.2, 5.1-5.2 [L] | 1,66 | 6 |
| 11 | 21 | 5.3 Diagonalization <br> - The diagonalization theorem <br> - Diagonalizating matrices <br> Midterm test on Chapters 3 and 4 | X |  | Book study, chapter 5-3 [L] | 1,66 |  |
| 11 | 22 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |


| 12 | 23 | 6. Orthogonality <br> 6.1 Inner product, length and orthogonality <br> 6.2 Orthogonal sets <br> - Orthogonal and ortonormal bases <br> - Orthogonal matrices | X |  | Book study, chapters 6.1-6.2 [L] | 1,66 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 24 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 13 | 25 | 6.3 Orthogonal projection <br> - The best approxiamtion theorem <br> 6.4 The Gram-Schmidt process | X |  | Book study, chapters 6.3-6.4 [L] | 1,66 | 6 |
| 13 | 26 | Selected exercises |  | X | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 14 | 27 | 6.5 Least squares problems <br> - Normal equations | X |  | Book study, chapter 6.5 [L] | 1,66 | 6 |
| 14 | 28 | Selected exercises | X |  | Odd numbered exercises. Compare with solutions (*) | 1,66 |  |
| 15 | 29 | 7. Diagonalization of symmetric matrices <br> - Th spectral theorem |  | X | Book study, chapter 7.1 [L] | 1,66 | 6 |
| 15 | 30 | Midterm test on Chapters 5 and 6 |  |  |  | 1,66 |  |
|  |  |  |  |  | Subtotal 1 | 50 | 90 |
|  |  |  | Total 1 (Hours of class plus student homework hours between weeks 1-15) |  |  | 140 |  |
|  |  | Assessment, evaluation preparation. Final Test |  |  |  | 3 | 7 |
|  |  |  |  |  | Subtotal 2 | 3 | 7 |
|  |  |  | Total 2 (Hours of class plus student homework hours between weeks 16-18) |  |  | 10 |  |
| TOTAL (Total 1 + Total 2) |  |  |  |  |  |  | 150 |

${ }^{(*)}$ Do some of the recomended exercises in W.K. Nicholson's ([N]) or D. C. Lay's ([L]) book corresponding to the previous lecture in large group and compare with the solutions in the book

