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## COURSE: CALCULUS II

## DEGREE: BACHELOR IN DATA SCIENCE AND ENGINEERING

28 sessions along 14 weeks

| WEEKLY PLANNING |  |  |  |  |  |  |  |
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| $\begin{aligned} & \sum_{\text {而 }} \end{aligned}$ |  | DESCRIPTION | GROUPS (mark X) |  | WEEKLY PROGRAMMING FOR STUDENT |  |  |
|  |  |  | LECTURES | SEMINARS | DESCRIPTION | CLASS HOURS | HOMEWORK HOURS <br> (Max. 7h week) |
| 1 | 1 | CHAPTER 1: DIFFERENTIAL CALCULUS IN SEVERAL VARIABLES <br> 1.1 $\mathrm{R}^{\mathrm{n}}$ as an Euclidean space; topology <br> 1.2 Functions of $n$ variables <br> - Functions, graphs, and level sets | X |  | Sections 14.1 and 16.2 [WHT] and/or sections 1.5, 2.1, 2.2 [MT] | 1,67 | 6,3 |
| 1 | 2 | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 2 | 3 | 1.3 Limits and Continuity | X |  | Section 14.2 [WHT] and/or section 2.2 [MT] | 1,67 | 6,3 |
| 2 | 4 | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 | 6, |
| 3 | 5 | 1.4 Differentiability <br> - Partial derivatives <br> - Derivative; Jacobian matrix | X |  | Section 14.3 [WHT] and/or section 2.3 [MT] | 1,67 | 6,3 |
| 3 | 6 | Test 1 <br> (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 4 | 7 | - Properties of the derivative <br> - Chain rule <br> - Directional derivatives; gradient vector | X |  | Sections 14.3-14.6 [WHT] and/or sections 2.5, 2.6 [MT] | 1,67 | 6,3 |
| 4 | 8 | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |

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| 5 | 9 | CHAPTER 2: LOCAL PROPERTIES OF FUNCTIONS <br> 2.1 Higher order derivatives <br> - Iterated derivatives; equality of mixed partials <br> - Differential operators: divergence, curl, Laplacian | X |  | Sections 16.4, 16.7, 16.8 [WHT] and/or sections 3.1, 3.2 [MT] | 1,67 | 6,3 |
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| 5 | 10 | Test 2 <br> (*) Discussion of selected exercises |  | X | $(* *)$ Problem solving for selected exercises | 1,67 |  |
| 6 | 11 | - Taylor polynomial; Hessian matrix <br> 2.2 Optimization <br> - Local extrema <br> - Absolute/global extrema | X |  | Sections 14.7, 14.9 [WHT] and/or sections 3.2, 3.3 [MT] | 1,67 | 6,3 |
| 6 | 12 | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 7 | 13 | - Free optimization problems <br> - Constrained optimization: Lagrange multipliers | X |  | Sections 14.7, 14.9 [WHT] and/or section 3.3, 3.4 [MT] | 1,67 | 6,3 |
| 7 | 14 | Test 3 <br> (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 8 | 15 | CHAPTER 3: INTEGRAL CALCULUS ON R ${ }^{\text {n }}$ <br> 3.1 Double and triple integrals <br> - Iterated integrals <br> - Cavalieri's principle <br> - Integrals over rectangular regions; Fubini's theorem | X |  | Sections 15.1, 15.5 [WHT] and/or sections 5.1-5.2 [MT] | 1,67 | 6,3 |
| 8 | 16 | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 9 | 17 | - Arbitrary 2- and 3-dimensional regions Change in the order of integration <br> 3.2 n-dimensional integrals | X |  | Sections 15.2, 15.3, 15.5 [WHT and/or sections 5.3-5.5 [MT] | 1,67 | 6,3 |
| 9 | 18 | Test 4 <br> (*) Discussion of selected exercises |  | X | $\left(^{* *}\right)$ Problem solving for selected exercises | 1,67 |  |
| 10 | 19 | 3.3 Changes of variables and applications <br> - Changes of variables; Jacobian <br> - Polar, cylindrical, and spherical coordinates <br> - Average; center of mass; moments of inertia | X |  | Sections 15.4, 15.6-15.8 [SHE] and/or sections 6.1-6.3 [MT] | 1,67 | 6,3 |
| 10 | 20 | (*) Discussion of selected exercises |  | X | $\left.{ }^{* *}\right)$ Problem solving for selected exercises | 1,67 |  |
| 11 | 21 | CHAPTER 4: INTEGRALS OVER CURVES AND SURFACES <br> 4.1 Line integrals <br> - Parametrized curves <br> - Line integral | X |  | Sections 16.1-16.3 [WHT] and/or sections 7.1, 7.2 [MT] | 1,67 | 6,3 |

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|  |  | - Conservative fields |  |  |  |  |  |  |
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| 11 | 22 | Test 5 <br> (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |  |
| 12 | 23 | 4.2 Surface integrals <br> - Parametrized surfaces <br> - Area of a Surface <br> - Integrals of scalar functions and vector fields | X |  | Sections 16.5, 16.6 [WHT] and/or sections 7.3-7.6 [MT] | 1,67 |  |  |
| 12 | 24 | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |  |
| 13 | 25 | 4.3 Integral theorems of vector analysis <br> - Planar case: Green's and divergence theorems <br> - Stokes' theorem | X |  | Sections 16.4, 16.7 [WHT] and/or sections 8.1, 8.2 [MT] | 1,67 | 6,3 |  |
| 13 | 26 | Test 6 <br> (*) Discussion of selected exercises |  | X | $\left.{ }^{* *}\right)$ Problem solving for selected exercises | 1,67 |  |  |
| 14 | 27 | - Conservative fields <br> - Gauss' theorem | X |  | Sections 16.7, 16.8 [WHT] and/or sections 8.3, 8.4 [MT] | 1,67 | 6,3 |  |
| 14 | 28 | (*) Discussion of selected exercises |  | X | $\left.{ }^{* *}\right)$ Problem solving for selected exercises | 1,67 | 6,3 |  |
| Subtotal 1 |  |  |  |  |  |  | 47 | 88 |
| Total 1 (Hours of class plus student homework hours between weeks 1-14) |  |  |  |  |  |  | 135 |  |



TOTAL (Total 1 + Total 2. Maximum 180 hours)

Notes:
[MT] Marsden and Tromba, "Vector Calculus", W. H. Freeman (6 ${ }^{\text {th }}$ edition, 2012)

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[WHT] Weir, Hass and Thomas, "Thomas' Calculus", Wiley (12 ${ }^{\text {th }}$ edition, 2009)
${ }^{(*)}$ Discussion of selected exercises from the course collection that correspond to the previous lecture
${ }^{(* *)}$ Problem solving for selected exercises from the course collection and sections of [MT], [WHT] that correspond to the previous lecture
(+) Lecture hours are always 1.67 ( 1.67 hours* 28 sessions $=46.76$ hours)

