## uc3m Universidad Carlos III de Madrid

## COURSE: CALCULUS II

## DEGREE: BACHELOR IN BIOMEDICAL ENGINEERING

ACADEMIC YEAR: 2020-2021
TERM: 2
28 sessions along 14 weeks
WEEKLY PLANNING

|  |  |  |  | WEEKLY PLA |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \sum_{\text {n }}^{\text {n }} \end{aligned}$ | $\begin{aligned} & \text { 资 } \\ & \frac{0}{2} \\ & \end{aligned}$ | DESCRIPTION | GROUPS (mark X) |  |
|  |  |  | LECTURES | SEminars |
| 1 | 4/02 | CHAPTER 1: DIFFERENTIAL CALCULUS IN SEVERAL VARIABLES <br> $1.1 \mathrm{R}^{\mathrm{n}}$ as an Euclidean space; topology <br> 1.2 Functions of $n$ variables <br> - Functions, graphs, and level sets | X |  |
| 1 | $\begin{gathered} 5 / 02 \\ \& \\ 10 / 02 \end{gathered}$ | (*) Discussion of selected exercises |  | X |
| 2 | 11/02 | 1.3 Limits and Continuity | X |  |
| 2 | $\begin{gathered} 12 / 02 \\ \& \\ 17 / 02 \end{gathered}$ | (*) Discussion of selected exercises |  | X |
| 3 | 18/02 | 1.4 Differentiability <br> - Partial derivatives <br> - Derivative; Jacobian matrix | X |  |
| 3 | $\begin{gathered} 19 / 02 \\ \& \\ 24 / 02 \end{gathered}$ | $\left(^{*}\right)$ Discussion of selected exercises |  | X |
| 4 | 25/02 | - Properties of the derivative <br> - Chain rule <br> - Directional derivatives; gradient vector | X |  |

WEEKLY PROGRAMMING FOR STUDENT
RS

| DESCRIPTION | CLASS HOURS | HOMEWORK HOURS <br> (Max. 7h week) |
| :--- | :---: | :---: |
| Sections 14.1 and 16.2 [WHT] and/or sections <br> $1.5,2.1,2.2[\mathrm{MT}]$ |  |  |
|  | 1,67 |  |

Sections 14.3-14.6 [WHT] and/or sections 2.5,
2.6 [MT]

1,67

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| 4 | $\begin{gathered} 26 / 02 \\ \& \\ 3 / 03 \\ \hline \end{gathered}$ | (*) Discussion of selected exercises |  | X | ${ }^{(* *)}$ Problem solving for selected exercises | 1,67 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 4/03 | CHAPTER 2: LOCAL PROPERTIES OF FUNCTIONS <br> 2.1 Higher order derivatives <br> - Iterated derivatives; equality of mixed partials <br> - Differential operators: divergence, curl, Laplacian | X |  | Sections 16.4, 16.7, 16.8 [WHT] and/or sections 3.1, 3.2 [MT] | 1,67 | 6,3 |
| 5 | $\begin{gathered} 5 / 03 \\ \& \\ 10 / 03 \end{gathered}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 6 | 11/03 | - Taylor polynomial; Hessian matrix 2.2 Optimization <br> - Local extrema <br> - Absolute/global extrema | X |  | Sections 14.7, 14.9 [WHT] and/or sections 3.2, 3.3 [MT] | 1,67 | 6,3 |
| 6 | $\begin{gathered} \hline 12 / 03 \\ \& \\ 17 / 03 \end{gathered}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 7 | 18/03 | - Free optimization problems <br> - Constrained optimization: Lagrange multipliers | X |  | Sections 14.7, 14.9 [WHT] and/or section 3.3, 3.4 [MT] | 1,67 |  |
| 7 | $\begin{array}{\|c} \hline 22 / 03 \\ \& \\ 24 / 03 \\ \hline \end{array}$ | First Mid term Exam |  | X |  | 1,67 | 6,3 |
| 8 | 25(03 | CHAPTER 3: INTEGRAL CALCULUS ON R ${ }^{\text {n }}$ <br> 3.1 Double and triple integrals <br> - Iterated integrals <br> - Cavalieri's principle <br> - Integrals over rectangular regions; Fubini's theorem | X |  | Sections 15.1, 15.5 [WHT] and/or sections 5.1-5.2 [MT] | 1,67 | 6,3 |
| 8 | $\begin{gathered} \hline 26 / 03 \\ \& \\ 7 / 04 \\ \hline \end{gathered}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |
| 9 | 8/04 | - Arbitrary 2- and 3-dimensional regions Change in the order of integration 3.2 n-dimensional integrals | X |  | Sections 15.2, 15.3, 15.5 [WHT and/or sections 5.3-5.5 [MT] | 1,67 | 6,3 |
| 9 | $\begin{gathered} 9 / 04 \\ \& \\ 14 / 04 \end{gathered}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |

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| 10 | 15/04 | 3.3 Changes of variables and applications <br> - Changes of variables; Jacobian <br> - Polar, cylindrical, and spherical coordinates <br> - Average; center of mass; moments of inertia | X |  | Sections 15.4, 15.6-15.8 [SHE] and/or sections 6.1-6.3 [MT] | 1,67 | 6,3 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | $\begin{gathered} 16 / 04 \\ \& \\ 21 / 04 \end{gathered}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |  |
| 11 | 22/04 | CHAPTER 4: INTEGRALS OVER CURVES AND SURFACES <br> 4.1 Line integrals <br> - Parametrized curves <br> - Line integral <br> - Conservative fields | X |  | Sections 16.1-16.3 [WHT] and/or sections 7.1, 7.2 [MT] | 1,67 | 6,3 |  |
| 11 | $\begin{gathered} \hline 23 / 04 \\ \& \\ 28 / 04 \\ \hline \end{gathered}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |  |
| 12 | 29/04 | 4.2 Surface integrals <br> - Parametrized surfaces <br> - Area of a Surface <br> - Integrals of scalar functions and vector fields | X |  | Sections 16.5, 16.6 [WHT] and/or sections 7.3-7.6 [MT] | 1,67 | 6,3 |  |
| 12 | $\begin{array}{\|c\|} \hline 30 / 04 \\ \& \\ 5 / 05 \\ \hline \end{array}$ | Second Mid Term Exam |  | X |  | 1,67 |  |  |
| 13 | 6/05 | 4.3 Integral theorems of vector analysis <br> - Planar case: Green's and divergence theorems <br> - Stokes' theorem | X |  | Sections 16.4, 16.7 [WHT] and/or sections 8.1, 8.2 [MT] | 1,67 | 6,3 |  |
| 13 | $\begin{array}{\|c} \hline 7 / 05 \\ \& \\ 12 / 05 \\ \hline \end{array}$ | (*) Discussion of selected exercises |  | X | (**) Problem solving for selected exercises | 1,67 |  |  |
| 14 | 13/05 | - Conservative fields <br> - Gauss' theorem | X |  | Sections 16.7, 16.8 [WHT] and/or sections 8.3, 8.4 [MT] | 1,67 |  |  |
| 14 | $\begin{array}{\|c} \hline 14 / 05 \\ \& \\ 19 / 05 \end{array}$ | $\left(^{*}\right)$ Discussion of selected exercises |  | X | ${ }^{* *}$ ) Problem solving for selected exercises | 1,67 |  |  |
| Total 1 (Hours of class plus student homework hours between weeks 1-14) Subtotal 1 |  |  |  |  |  |  | 47 | 88 |
|  |  |  |  |  |  |  | 135 |  |

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Notes:
[MT] Marsden and Tromba, "Vector Calculus", W. H. Freeman ( $6^{\text {th }}$ edition, 2012)
[WHT] Weir, Hass and Thomas, "Thomas' Calculus", Wiley ( $12^{\text {th }}$ edition, 2009)
(*) Discussion of selected exercises from the course collection that correspond to the previous lecture
(**) Problem solving for selected exercises from the course collection and sections of [MT], [WHT] that correspond to the previous lecture
(+) Lecture hours are always 1.67 ( 1.67 hours* 28 sessions $=46.76$ hours)

