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COURSE: CALCULUS II

DEGREE: BACHELOR IN BIOMEDICAL ENGINEERING ACADEMIC YEAR: 2020-2021 TERM: 2

28 sessions along 14 weeks

| WEEKLY PLANNING | | | | | | | | |
|-----------------|---------------------|--|--------------------|----------|---|-------------|----------------------------------|--|
| WEEK | SESSION | DESCRIPTION | GROUPS (mark X) | | WEEKLY PROGRAMMING FOR STUDENT | | | |
| | | | LECTURES | SEMINARS | DESCRIPTION | CLASS HOURS | HOMEWORK HOURS (Max. 7h week) | |
| | | CHAPTER 1: DIFFERENTIAL CALCULUS IN SEVERAL VARIABLES | | | Sections 14.1 and 16.2 [WHT] and/or sections 1.5, 2.1, 2.2 [MT] | | | |
| 1 | 4/02 | 1.1 Rⁿ as an Euclidean space; topology 1.2 Functions of n variables Functions, graphs, and level sets | X | | | 1,67 | 6,3 | |
| 1 | 5/02 & 10/02 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | | |
| 2 | 11/02 | 1.3 Limits and Continuity | Х | | Section 14.2 [WHT] and/or section 2.2 [MT] | 1,67 | | |
| 2 | 12/02 & 17/02 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | 6,3 | |
| 3 | 18/02 | 1.4 Differentiability | х | | Section 14.3 [WHT] and/or section 2.3 [MT] | 1,67 | 6,3 | |
| 3 | 19/02 & 24/02 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | 0,3 | |
| 4 | 25/02 | Properties of the derivative Chain rule Directional derivatives; gradient vector | Х | | Sections 14.3-14.6 [WHT] and/or sections 2.5, 2.6 [MT] | 1,67 | 6,3 | |

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| 4 | 26/02 & 3/03 | (*) Discussion of selected exercises | | х | (**) Problem solving for selected exercises | 1,67 | |
|---|---------------------|---|---|---|---|------|-----|
| 5 | 4/03 | CHAPTER 2: LOCAL PROPERTIES OF FUNCTIONS 2.1 Higher order derivatives - Iterated derivatives; equality of mixed partials - Differential operators: divergence, curl, Laplacian | Х | | Sections 16.4, 16.7, 16.8 [WHT] and/or sections 3.1, 3.2 [MT] | 1,67 | 6,3 |
| 5 | 5/03 & 10/03 | | | Х | (**) Problem solving for selected exercises | 1,67 | |
| 6 | 11/03 | Taylor polynomial; Hessian matrix 2.2 Optimization Local extrema Absolute/global extrema | X | | Sections 14.7, 14.9 [WHT] and/or sections 3.2, 3.3 [MT] | 1,67 | 6,3 |
| 6 | 12/03 & 17/03 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | |
| 7 | 18/03 | Free optimization problemsConstrained optimization: Lagrange multipliers | Х | | Sections 14.7, 14.9 [WHT] and/or section 3.3, 3.4 [MT] | 1,67 | |
| 7 | 22/03 & 24/03 | First Mid term Exam | | х | | 1,67 | 6,3 |
| 8 | 25(03 | CHAPTER 3: INTEGRAL CALCULUS ON R ⁿ 3.1 Double and triple integrals - Iterated integrals - Cavalieri's principle - Integrals over rectangular regions; Fubini's theorem | х | | Sections 15.1, 15.5 [WHT] and/or sections 5.1-5.2 [MT] | 1,67 | 6,3 |
| 8 | 26/03 & 7/04 | (*) Discussion of selected exercises | | х | (**) Problem solving for selected exercises | 1,67 | |
| 9 | 8/04 | Arbitrary 2- and 3-dimensional regions Change in the order of integration 3.2 n-dimensional integrals | Х | | Sections 15.2, 15.3, 15.5 [WHT and/or sections 5.3-5.5 [MT] | 1,67 | 6,3 |
| 9 | 9/04 & 14/04 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | |

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| | | Total 1 (Hours of o | class plus stu | dent homew | vork hours between weeks 1-14) | | 135 | |
|----|---------------------|---|----------------|------------|---|------------|-----|----|
| | | | • | • | | Subtotal 1 | 47 | 88 |
| 14 | 14/05 & 19/05 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | 6,3 | |
| 14 | 13/05 | Conservative fieldsGauss' theorem | Х | | Sections 16.7, 16.8 [WHT] and/or sections 8.3, 8.4 [MT] | 1,67 | 6,3 | |
| 13 | 7/05 & 12/05 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | 5,5 | |
| 13 | 6/05 | 4.3 Integral theorems of vector analysis - Planar case: Green's and divergence theorems - Stokes' theorem | Х | | Sections 16.4, 16.7 [WHT] and/or sections 8.1, 8.2 [MT] | 1,67 | 6,3 | |
| 12 | 30/04 & 5/05 | Second Mid Term Exam | | Х | | 1,67 | | |
| 12 | 29/04 | 4.2 Surface integrals Parametrized surfaces Area of a Surface Integrals of scalar functions and vector fields | х | | Sections 16.5, 16.6 [WHT] and/or sections 7.3-7.6 [MT] | 1,67 | 6,3 | |
| 11 | 23/04 & 28/04 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | | |
| 11 | 22/04 | CHAPTER 4: INTEGRALS OVER CURVES AND SURFACES 4.1 Line integrals - Parametrized curves - Line integral - Conservative fields | х | | Sections 16.1-16.3 [WHT] and/or sections 7.1, 7.2 [MT] | 1,67 | 6,3 | |
| 10 | 16/04 & 21/04 | (*) Discussion of selected exercises | | Х | (**) Problem solving for selected exercises | 1,67 | | |
| 10 | 15/04 | 3.3 Changes of variables and applications Changes of variables; Jacobian Polar, cylindrical, and spherical coordinates Average; center of mass; moments of inertia | х | | Sections 15.4, 15.6-15.8 [SHE] and/or sections 6.1-6.3 [MT] | 1,67 | 6,3 | |

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| TOTAL (Total 1 + Total 2. Maximum 180 hours) | | | | | | 150 | | |
|--|------------------------------------|--|--|--|--|------------|----|----|
| Total 2 (Hours of class plus student homework hours between weeks 15-18) | | | | | | 15 | | |
| | | | | | | Subtotal 2 | 3 | 12 |
| 18 | | | | | | | | |
| 17 | Assessment, final exam preparation | | | | | 3 | 10 | |
| 16 | | | | | | | | |
| 15 | Tutorials, handing-in, etc. | | | | | | 2 | |

Notes:

[MT] Marsden and Tromba, "Vector Calculus", W. H. Freeman (6th edition, 2012) [WHT] Weir, Hass and Thomas, "Thomas' Calculus", Wiley (12th edition, 2009)

- (*) Discussion of selected exercises from the course collection that correspond to the previous lecture
- (**) Problem solving for selected exercises from the course collection and sections of [MT], [WHT] that correspond to the previous lecture
- (+) Lecture hours are always 1.67 (1.67 hours*28 sessions = 46.76 hours)