## uc3m Universidad Carlos III de Madrid

**COURSE: CALCULUS II** 

DEGREE: BACHELOR IN BIOMEDICAL ENGINEERING ACADEMIC YEAR: 2019-2020 TERM: 2

28 sessions along 14 weeks

	WEEKLY PLANNING							
WEEK	SESSION	DESCRIPTION	GROUPS (mark X)		WEEKLY PROGRAMMING FOR STUDENT			
			LECTURES	SEMINARS	DESCRIPTION	CLASS HOURS	HOMEWORK HOURS (Max. 7h week)	
1	1	CHAPTER 1: DIFFERENTIAL CALCULUS IN SEVERAL VARIABLES	V		Sections 14.1 and 16.2 [WHT] and/or sections 1.5, 2.1, 2.2 [MT]	1.67		
1	1	<ul> <li>1.1 R<sup>n</sup> as an Euclidean space; topology</li> <li>1.2 Functions of n variables</li> <li>Functions, graphs, and level sets</li> </ul>	X			1,67	6,3	
1	2	(*) Discussion of selected exercises		X	(**) Problem solving for selected exercises	1,67		
2	3	1.3 Limits and Continuity	Х		Section 14.2 [WHT] and/or section 2.2 [MT]	1,67	6,3	
2	4	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	0,5	
3	5	1.4 Differentiability	Х		Section 14.3 [WHT] and/or section 2.3 [MT]	1,67	6,3	
3	6	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67		
4	7	<ul> <li>Properties of the derivative</li> <li>Chain rule</li> <li>Directional derivatives; gradient vector</li> </ul>	х		Sections 14.3-14.6 [WHT] and/or sections 2.5, 2.6 [MT]	1,67	6,3	
4	8	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67		
5	9	CHAPTER 2: LOCAL PROPERTIES OF FUNCTIONS 2.1 Higher order derivatives	Х		Sections 16.4, 16.7, 16.8 [WHT] and/or	1,67	6,3	

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		<ul> <li>Iterated derivatives; equality of mixed partials</li> <li>Differential operators: divergence, curl, Laplacian</li> <li>Test 2</li> </ul>			sections 3.1, 3.2 [MT]		
5	10	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
6	11	<ul> <li>Taylor polynomial; Hessian matrix</li> <li>2.2 Optimization</li> <li>Local extrema</li> <li>Absolute/global extrema</li> </ul>	Х		Sections 14.7, 14.9 [WHT] and/or sections 3.2, 3.3 [MT]	1,67	6,3
6	12	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
7	13	<ul> <li>Free optimization problems</li> <li>Constrained optimization: Lagrange multipliers</li> <li>Test 3</li> </ul>	Х		Sections 14.7, 14.9 [WHT] and/or section 3.3, 3.4 [MT]	1,67	6,3
7	14	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
8	15	CHAPTER 3: INTEGRAL CALCULUS ON R <sup>n</sup> 3.1 Double and triple integrals  - Iterated integrals  - Cavalieri's principle  - Integrals over rectangular regions; Fubini's theorem	х		Sections 15.1, 15.5 [WHT] and/or sections 5.1-5.2 [MT]	1,67	6,3
8	16	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
9	17	<ul> <li>Arbitrary 2- and 3-dimensional regions</li> <li>Change in the order of integration</li> <li>3.2 n-dimensional integrals</li> <li>Test 4</li> </ul>	Х		Sections 15.2, 15.3, 15.5 [WHT and/or sections 5.3-5.5 [MT]	1,67	6,3
9	18	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
10	19	<ul> <li>3.3 Changes of variables and applications</li> <li>Changes of variables; Jacobian</li> <li>Polar, cylindrical, and spherical coordinates</li> <li>Average; center of mass; moments of inertia</li> </ul>	Х		Sections 15.4, 15.6-15.8 [SHE] and/or sections 6.1-6.3 [MT]	1,67	6,3
10	20	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	
11	21	CHAPTER 4: INTEGRALS OVER CURVES AND SURFACES  4.1 Line integrals  - Parametrized curves  - Line integral  - Conservative fields  Test 5	Х		Sections 16.1-16.3 [WHT] and/or sections 7.1, 7.2 [MT]	1,67	6,3

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11	22	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67		
12	23	<ul> <li>4.2 Surface integrals</li> <li>Parametrized surfaces</li> <li>Area of a Surface</li> <li>Integrals of scalar functions and vector fields</li> </ul>	×		Sections 16.5, 16.6 [WHT] and/or sections 7.3-7.6 [MT]	1,67	6,3	
12	24	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67		
13	25	4.3 Integral theorems of vector analysis  - Planar case: Green's and divergence theorems  - Stokes' theorem  Test 6	х		Sections 16.4, 16.7 [WHT] and/or sections 8.1, 8.2 [MT]	1,67	6,3	
13	26	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67		
14	27	<ul><li>Conservative fields</li><li>Gauss' theorem</li></ul>	Х		Sections 16.7, 16.8 [WHT] and/or sections 8.3, 8.4 [MT]	1,67	6,3	
14	28	(*) Discussion of selected exercises		Х	(**) Problem solving for selected exercises	1,67	6,3	
						Subtotal 1	47	88
Total 1 (Hours of class plus student homework hours between weeks 1-14)						135		
15		Tutorials, handing-in, etc.					2	
16								
17		Assessment, final exam preparation				3	10	
18								
						Subtotal 2	3	12
Total 2 (Hours of class plus student homework hours between weeks 15-18)						15		
TOTAL (Total 1 + Total 2. Maximum 180 hours)						150		

## Notes:

[MT] Marsden and Tromba, "Vector Calculus", W. H. Freeman (6<sup>th</sup> edition, 2012) [WHT] Weir, Hass and Thomas, "Thomas' Calculus", Wiley (12<sup>th</sup> edition, 2009)

- (\*) Discussion of selected exercises from the course collection that correspond to the previous lecture
- (\*\*) Problem solving for selected exercises from the course collection and sections of [MT], [WHT] that correspond to the previous lecture
- (+) Lecture hours are always 1.67 (1.67 hours\*28 sessions = 46.76 hours)