Advanced Stochastic Processes

Academic Year: (2023 / 2024)

Department assigned to the subject: Statistics Department

Coordinating teacher: MEILAN VILA, ANDREA

Type: Electives ECTS Credits : 6.0

Year : 4 Semester :

REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Stochastic Processes

DESCRIPTION OF CONTENTS: PROGRAMME

- 1 Brownian motion
- 1.1 Definition and properties
- 1.2 Derived Processes
- 1.3 Simulation
- 2 Martingales in continuous time
- 2.1 Definition and properties
- 2.2 Optional sampling theorem
- 3 Stochastic Integration
- 3.1 Definition and properties
- 3.2 Lema of Itô
- 3.3 Girsanov's theorem
- 3.4 Martingale Representation Theorem
- 4 Introduction to differential stochastic equations
- 4.1 Itô's Stochastic Differential Equations
- 4.2 Linear Differential Equations
- 4.3 Digital solutions
- 5 Applications of stochastic calculus to Finance
- 5.1 The Black-Scholes formula
- 5.2 Risk neutral measures
- 5.3 Pricing Exotic options
- 5.4 Pricing American options

LEARNING ACTIVITIES AND METHODOLOGY

Theory (4 ECTS). Lectures. Practice (2 ECTS). Problem solving lessons.

ASSESSMENT SYSTEM

The subject will be evaluated through two partial exams (50% each of them).

% end-of-term-examination:	0
% of continuous assessment (assigments, laboratory, practicals):	100

BASIC BIBLIOGRAPHY

- H. Bühlmann Mathematical Methods in Risk Theory., Springer, 1996 (2nd. ed)

- R. Durrett Essentials of stochastic processes, Springer, 2012 (2nd ed.)
- S. Asmussen and H. Albrecher Ruin Probabilities, World Scientific, 2010 (2nd. ed.)
- S.M. Ross Stochastic Processes, John Wiley & Sons, inc., 1996 (2nd. ed.)

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BASIC ELECTRONIC RESOURCES

- R. Durrett . Essentials of Stochastic Processes: http://www.math.duke.edu/~rtd/EOSP/EOSP2E.pdf