

Academic Year: (2023 / 2024)

Review date: 11-05-2023

Department assigned to the subject: Mathematics Department

Coordinating teacher: TERRAGNI , FILIPPO

Type: Basic Core ECTS Credits : 6.0

Year : 2 Semester :

Branch of knowledge: Engineering and Architecture

REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Calculus (Course 1 - Semester 1)

Linear Algebra (Course 1 - Semester 1)

SKILLS AND LEARNING OUTCOMES

- ¿ Solve linear and non-linear first-order ordinary differential equations and second-order linear ordinary differential equations and interpret the results
- ¿ Understand the concept of Fourier series and Laplace transform and apply them to the solution of differential equations.
- ¿ Solve systems of first order linear differential equations.
- ¿ Use numerical methods to calculate approximate solutions of non-linear differential equations.

OBJECTIVES

The objective of the course is to provide the student with the necessary tools to understand the scientific and mathematical principles of computer engineering.

DESCRIPTION OF CONTENTS: PROGRAMME

- 1.- First order differential equations:
 - a. Introduction.
 - b. Separable equations.
 - c. Linear equations.
 - d. Exact equations.
 - e. Homogeneous equations.
- 2.- Second order differential equations.
 - a. Linear and nonlinear equations.
 - b. Homogeneous and non-homogeneous linear Equations.
 - c. Reduction of order.
 - d. Euler-Cauchy equations.
- 3.- The Laplace Transform:
 - a. Definition. Properties.
 - b. Application to differential equations.
- 4.- Systems of differential equations:
 - a. Linear and nonlinear systems.
 - b. Vectorial representation.
 - c. Eigenvalues and linearization.
5. Fourier series and separation of variables:
 - a. Basic results.
 - b. Fourier Sine and Cosine Series.
 - c. Applications of Fourier series and separation of variables to partial differential equations.
- 6.- Numerical methods:
 - a. Euler method.
 - b. Runge-Kutta method.
 - c. Boundary value problems.

- 1.- Teaching in big or aggregate groups. Lectures sessions (3 ECTS).
- 2.- Face-to-face teaching in small groups. Problem sessions with individual and group work (3 ECTS).

Office hours: Each teacher offers a number of office hours according to the regulations of the Carlos III University. In particular, a minimum of one hour per group with the time schedule compatible with the students.

ASSESSMENT SYSTEM

We follow a continuous-assessment system (40%) plus a final exam (60%) :

- The continuous-assessment part consists in two mid-term exams that will be held in regular class hours, according to the current regulations and will contribute a weight of 40% to the final mark. These mid-term tests allow the students to modify their own learning strategies, if necessary.
- The final exam (contributing with weight 60% to the final mark) will be held at the end of the semester, and allows to assess globally the knowledge of the course topics, skills, and capabilities acquired by the students.
- There is an extraordinary final exam in June for those students who did not obtain the required end-of-semester mark. This extraordinary final exam has a maximum mark of 10, and the June final mark is given by $\max(EE, 0.6 EE + 0.4 CA)$, where EE (resp. CA) is the extraordinary final-exam (resp. continuous-assessment) mark.

% end-of-term-examination:	60
% of continuous assessment (assignments, laboratory, practicals...):	40

BASIC BIBLIOGRAPHY

- Boyce, William E. Elementary differential equations and boundary value problems , John Wiley & Sons,.
- Simmons, George Finlay Differential equations with applications and historical notes., McGraw-Hill.
- Zill, Dennis G. Ecuaciones diferenciales con aplicaciones de modelado , International Thomson.

ADDITIONAL BIBLIOGRAPHY

- Haberman, Richard Elementary applied partial differential equations with Fourier series and boundary value problems 3rd ed, Prentice Hall.
- Gockenbach, Mark S. Partial differential equations : analytical and numerical methods, SIAM.
- Kiseliov, Aleksandr I. Problemas de ecuaciones diferenciales ordinarias , Mir.
- Weinberger, Hans F. A first course in partial differential equations with complex variables and transform methods, Dover.

BASIC ELECTRONIC RESOURCES

- Manuel Carretero, Luis L. Bonilla, Filippo Terragni, Segei Iakunin, Rocío Vega . Course OCW-UC3M Applied Differential Calculus: <http://ocw.uc3m.es/matematicas/applied-differential-calculus>