Advanced Mathematics II

Academic Year: (2023 / 2024)

Department assigned to the subject: Mathematics Department

Coordinating teacher: ARVESU CARBALLO, JORGE

Type: Electives ECTS Credits : 6.0

Year : Semester :

# REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Linear algebra, Calculus I

## **OBJECTIVES**

- 1. Basic numerical skills to solve problems in Engineering.
- 2. The use of MATLAB to solve numerical problems.
- 3. Basic solving skills to solve counting problems.
- 4. Basic solving skills to solve discrete mathematics.

# DESCRIPTION OF CONTENTS: PROGRAMME

- 0: Algorithms and Complexity
- 0.1 The Growth of Functions
- 0.2 Complexity of Algorithms
- 0.3 Representations of Integers
- 1: Floating-Point Numbers and Errors
- 1.1 Floating-Point Numbers
- 1.2 Floating-Point Numbers in Matlab
- 1.3 Floating-Point Arithmetic
- 2: Integers
- 2.1 Divisibility and Modular Arithmetic
- 2.2 Integer Representations and Algorithms
- 2.3 Primes and Greatest Common Divisors
- 2.4 Solving Congruences. The Chinese Reminder Theorem
- 3: Counting
- 3.1 The Basics of Counting
- 3.2 The Pigeonhole Principle
- 3.3 Permutations and Combinations
- 4: Linear Equations
- 4.1 Solving Linear Systems
- 4.2 LU Factorization
- 4.3 Pivoting and Permutation Matrices
- 4.4 Effect of Roundoff Errors
- 4.5 lutx
- 5: Interpolation
- 5.1 The Interpolating Polynomial
- 5.2 Piecewise Linear Interpolation
- 5.3 Piecewise Cubic Interpolation
- 5.4 splinetx y pchiptx
- 6: Zeros and Roots
- 6.1 Bisection
- 6.2 Convergence Rates
- 6.3 Newton's and Secant methods
- 6.4 Inverse cuadratic interpolation
- 6.5 Brent¿s algorithm and fzerotx

Review date: 11-05-2023

7: Quadrature7.1 Simple and composite quadrature rules7.2 Adaptive Quadrature. quadtx7.3 Gaussian Quadrature

8: Least Squares 8.1 Models and Curve Fitting 8.2 Least Squares and QR

# LEARNING ACTIVITIES AND METHODOLOGY

There will be two weakly sessions:

- Theory sessions: the teacher will explain the fundamental concepts and results of the theory.

- Exercise/Lab sessions: the students will work in solving exercises or writing codes to solve problems proposed by the teacher.

## ASSESSMENT SYSTEM

Final exam: 50% Midterm exams: 25% Homeworks: 25%

% end-of-term-examination:	50
% of continuous assessment (assigments, laboratory, practicals):	50

## BASIC BIBLIOGRAPHY

- C. Moler Numerical Computing with MATLAB, SIAM, 2004
- D. J. Higham N. J. Higham Matlab Guide, SIAM, 2000
- J.H. Mathews y K.D. Fink Mumerical Methods with Matlab, 3rd ed, Prentice Hall, 2000
- K.H. Rosen Discrete Mathematics and applications, McGraw-Hill, 2004
- T. Sauer Análisis Numérico 2ed, Pearson, 2013

## ADDITIONAL BIBLIOGRAPHY

- B. Kolman, R. C. Busby, S. Ross Discrete Mathematical Structures (6th Edition), Pearson Educación, 1997
- G. W. Stewart Afternotes on Numerical Analysis, SIAM, 1996
- G. W. Stewart Afternotes goes to Graduate School, SIAM, 1998
- J.M. Sanz-Serna Diez Lecciones de Cálculo Numérico, Universidad de Valladolid, 2010
- R. Johnsonbaugh Discrete Mathematics, 4rd ed., Prentice-Hall, 1999