# uc3m Universidad Carlos III de Madrid

# Elementary statistical theory II

Academic Year: (2023 / 2024) Review date: 04-05-2023

Department assigned to the subject: Statistics Department Coordinating teacher: JIMENEZ RECAREDO, RAUL JOSE

Type: Basic Core ECTS Credits: 6.0

Year: 1 Semester: 2

Branch of knowledge: Social Sciences and Law

# REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Teoría Estadística Elemental I

#### **OBJECTIVES**

#### SPECIFIC COMPETENCES

- 1. Understand the concept of random vector: description and applications.
- 2. Use the concept of correlation.
- 3. Work with the multivariate normal distribution.
- 4. Use the limit theorems and asymptotic results in statistical applications.
- 5. Understand the concept of statistics and its sampling distribution.
- 6. Obtain the sampling distribution of estimators in normal population and derive the associated confidence intervals.
- 7. Use computational tools for calculation of confidence intervals.

#### CROSS COMPETENCES

- 1. Information Management Skills.
- 2. Solve Problems independently.
- 3. To be capable of using creative thoughts when it comes to solve problems.
- 4. Critical Reasoning.

## **DESCRIPTION OF CONTENTS: PROGRAMME**

- 1. Discrete random vectors.
- 1.1. Joint, marginal and conditional distributions.
- 1.2. Independence.
- 1.3. Functions of random vectors.
- 1.4. Expected value and variance, conditional expectation.
- 1.5. Discrete multivariate models.
- 2. Continuous Random vectors.
- 2.1. Joint, marginal and conditional distributions.
- 2.2. Independence. Functions of random vectors.
- 2.3. Change of variable.
- 2.4. Expected value and variance, conditional expectation.
- 2.4. Bimensional normal distribution.
- 3. Introduction to statistical inference.
- 3.1. Simple random samples.
- 3.2. Markov inequality and weak law of large numbers.
- 3.3. Central Limit Theorem.
- 3.4. Sampling distributions based on normal populations (chi-square and Student t test).
- 3.5. Confidence intervals.

## LEARNING ACTIVITIES AND METHODOLOGY

Theory (4 ECTS). Lectures with available material posted in internet. Problems (2 ECTS) Problem Solving classes. Work assignments in groups.

## ASSESSMENT SYSTEM

Final exam 50%. tests, labs homework exercises 50%.

% end-of-term-examination: 50

% of continuous assessment (assigments, laboratory, practicals...): 50

#### **BASIC BIBLIOGRAPHY**

- Casella, G. y Berger, R.L. Statistical Inference, Wadsworth and brooks. 1990.
- Durá Peiró, J.M. y López Cuñat, J. Fundamentos de Estadística. Estadística descriptiva y modelos probabilísticos para la Inferencia, Ed. Ariel. 1992.
- Lipschutz, S. y Schiller, J. Introducción a la Probabilidad y Estadística, Mc Graw-Hill. 2001.
- Mendenhall, Scheaffer y Wackerly Estadística matemática con Aplicaciones, Ed. Grupo editorial Iberoamericana. 1986.
- Peña, D. Introducción a la Estadística, Ed. Alianza Editorial. 2002.

## ADDITIONAL BIBLIOGRAPHY

- Durret, R. The Essentials of Probability, Duxbury Press. 1994.
- Grimmett, G. y D. J. A. Welsh. Probability: An introduction., Oxford University Press, 2003