# uc3m Universidad Carlos III de Madrid

## Calculus III

Academic Year: (2022 / 2023) Review date: 21-09-2022

Department assigned to the subject: Mathematics Department Coordinating teacher: CASTILLO RIVERA, SALVADOR

Type: Compulsory ECTS Credits: 6.0

Year: 2 Semester: 1

## REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Calculus I, Calculus II, Linear Algebra.

#### **OBJECTIVES**

By the end of this course, students will be able to:

- 1. Know and understand the mathematical principles of the Theory of Differential Equations, both Ordinary and in Partial Derivatives, underlying Energy Engineering.
- 2. Apply their knowledge and understanding of the mathematical principles to identify, formulate and solve problems in Differential Equations by using established methods.
- 3. Combine theory and practice to solve Differential Equations problems.
- 4. Know and understand the methods and procedures of the Theory of Differential Equations, its area of application and its limitations.

## **DESCRIPTION OF CONTENTS: PROGRAMME**

- 1. First Order Differential Equations.
  - a. Definitions and examples.
  - b. Elementary resolution methods.
  - c. Applications.
- 2. Higher Order Linear Differential Equations.
  - a. Linear equations of order n with constant coefficients.
  - b. Equations with variable coefficientes: undetermined coefficients and variation of constants
- 3. Laplace Transform.
  - a. Definition and properties.
  - b. Transforming and anti-transforming.
  - c. Application to solving linear differential equations and systems.
- 4. Introduction to Partial Differential Equations.
  - a. Initial and boundary problems.
  - b. Examples of PDEs of Mathematical Physics.
  - c. Different kind of equations and data.
  - d. Classification of second order, linear PDEs.
- 5. Method of separation of variables.
  - a. Even, odd, and periodic extensiones of a function. Trigonometric Fourier series.
  - b. Solving homogeneous and non-homogeneous PDEs using separation of variables and Fourier series.
- 6. Sturm-Liouville Problems.
  - a. Self-adjoint Sturm-Liouville problems.
  - b. Rayleigh's quotient. Minimization theorem.
  - c. Solving PDEs using separation of variables and generalized Fourier series.

## LEARNING ACTIVITIES AND METHODOLOGY

The learning methodology consists of:

- -lectures covering the most important topics defined in the course programe.
- -Participation at class solving proposed problems in group or individually on the blackboard.

#### ASSESSMENT SYSTEM

- 1. Control exams.
- 2. Final exam.

% end-of-term-examination: 60 % of continuous assessment (assignments, laboratory, practicals...): 40

#### **BASIC BIBLIOGRAPHY**

- G.F. SIMMONS, S.G. KRANTZ Differential Equations, Theory, Technique and Practice, McGraw-Hill Companies Inc., 2007
- R. HABERMAN Elementary Applied Partial Differential Equations, Prentice Hall, 3rd. edition, 1998

## ADDITIONAL BIBLIOGRAPHY

- C.H.EDWARDS Jr., D.E. PENNEY Ecuaciones Diferenciales Elementales y Problemas con Condiciones en la Frontera, 3ª edición, Prentice-Hall, 1993
- D.G. ZILL. Ecuaciones Diferenciales con Aplicaciones de Modelado,, Thomson, sexta edición, 1997
- G.F. SIMMONS Ecuaciones Diferenciales con Aplicaciones y Notas Históricas, McGraw-Hill, 1993
- J.R. BRANNAN, W.E. BOYCE Differential Equations with Boundary Value Problems: An Introduction to Methods and Applications, Wiley, 2010
- R.K. NAGLE, R. KENT, E.B. SAFF, A.D. SNIDER Fundamentals of Differential Equations, Pearson Addison-Wesley, 7th ed. 2008
- W.E. BOYCE, R.C. DI PRIMA. Ecuaciones Diferenciales y Problemas con Valores en la Frontera. , Limusa, 1998