

Academic Year: ( 2022 / 2023 )

Review date: 19-05-2022

Department assigned to the subject: Mathematics Department

Coordinating teacher: MORO CARREÑO, JULIO

Type: Basic Core ECTS Credits : 6.0

Year : 2 Semester : 1

Branch of knowledge: Engineering and Architecture

**REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)**

Calculus I and II, and Linear Algebra

**DESCRIPTION OF CONTENTS: PROGRAMME**

## 1. Arithmetic

- 1.1 Integers
- 1.2 Division algorithm
- 1.3 Largest common divisor: Euclid's algorithm
- 1.4 Prime numbers and the Fundamental Theorem of Arithmetic
- 1.5 Diophantine equations
- 1.6 Congruences: modular arithmetic

## 2. Elementary set theory

- 2.1 Basic notions
- 2.2 Set operations and properties
- 2.3 Functions
- 2.4 Relations: equivalence and order
- 2.5 Cardinality

## 3. Combinatorics

- 3.1 Elementary counting rules: sum and product
- 3.2 Pigeon-hole principle
- 3.3 Permutations and combinations
- 3.4 Binomial coefficients
- 3.5 Principle of inclusion and exclusion
- 3.6 Derangements
- 3.7 Generating functions
- 3.8 Partitions
- 3.9 Recurrences

## 4. Introduction to groups

- 4.1 Law of composition
- 4.2 Groups and subgroups
- 4.3 Homomorphisms and isomorphisms
- 4.4 Cyclic groups
- 4.5 Cosets, Lagrange's theorem, and quotient groups
- 4.6 Applications to cryptography

## 5. Fundamentals of graph theory

- 5.1 Definitions and examples
- 5.2 Matrix representations
- 5.3 Eulerian and Hamiltonian graphs
- 5.4 Trees
- 5.5 Optimisation and matching

- 5.6 Planar graphs
- 5.7 Directed graphs
- 5.8 Networks

## LEARNING ACTIVITIES AND METHODOLOGY

AF1: THEORETICAL AND PRACTICAL LECTURES. These are meant to provide the students the basic knowledge of the topic. They will be provided classroom notes as well as reference textbooks to help them follow the lectures and work them through. Exercises and problems will be solved in class, and midterm exams will be performed to test progress.

AF3: PERSONAL WORK AND WORK IN GROUPS.

AF9: FINAL EXAM. Overall evaluation of the students' knowledge, skills, and abilities learn through the course.

MD1: THEORY CLASS. The teacher will lecture, with the help of computer and audiovisual media, about the main topics of the subject. Materials and bibliography will be provided to supplement these lectures.

MD2: PRACTICAL CLASS. Practical exercises and problems will be solved, either individually or in groups.

MD3: TUTORSHIPS. The student will receive assistance by the teacher about difficult matters of the topic, either individually or in groups.

## ASSESSMENT SYSTEM

SE1: FINAL EXAM. Overall evaluation of the students' knowledge, skills, and abilities learn through the course.

SE2: CONTINUOUS EVALUATION. Several tests will be performed along the course to evaluate the most recent topics explained in class.

<b>% end-of-term-examination:</b>	60
<b>% of continuous assessment (assignments, laboratory, practicals...):</b>	40

## BASIC BIBLIOGRAPHY

- K.H. Rosen Discrete Mathematics and Its Applications, 7th ed., McGraw-Hill, 2007
- N. Biggs Discrete Mathematics, 2nd ed., Oxford University Press, 2003
- R.P. Grimaldi Discrete and Combinatorial Mathematics: An Applied Introduction, 5th ed., Addison Wesley, 2004

## ADDITIONAL BIBLIOGRAPHY

- M. E. J. Newman Networks: An Introduction, Oxford University Press, 2010
- N. C. Carter Visual Group Theory, Mathematical Association of America, Inc., 2009
- R. J. Wilson Introduction to Graph Theory, 4th ed., Addison-Wesley, 1996
- R. Sedgewick, P. Flajolet An introduction to the analysis of algorithms, 2nd ed., Addison-Wesley, 2013