uc3m Universidad Carlos III de Madrid

Probability

Academic Year: (2022 / 2023) Review date: 20-05-2022

Department assigned to the subject: Statistics Department

Coordinating teacher: ARRIBAS GIL, ANA Type: Compulsory ECTS Credits: 3.0

Year: 1 Semester: 1

OBJECTIVES

Knowledge acquisition of: 1) random variables, elementary probability and distributions; 2) relevant probabilistic inequalities; 3) random vectors, marginal and joint distributions; 4) sequences of random variables and concepts of convergences;

DESCRIPTION OF CONTENTS: PROGRAMME

- 1. Random experiments
- 1.1 Events
- 1.2 Probability
- 1.3 Conditional probability
- 1.4 Bayes' formula
- 1.5 Independence
- 1.6 Combinatorics
- 2. Discrete random Variables
- 2.1 Definition of random variable
- 2.2 Probability mass function and cumulative distribution function
- 2.3 Mean, variance, and quantiles
- 2.4 Binomial, Geometric, Poisson, Negative Binomial, and Hypergeometric distributions
- 3. Continuous random variables
- 3.1 Density mass function and cumulative distribution function
- 3.2 Mean, variance, and quantiles
- 3.3 Transformations of a random variable
- 3.4 Uniform, Exponential, Normal, Gamma, and Beta distributions
- 4. Random vectors
- 4.1 Joint distributions, marginal distributions, and conditional distributions
- 4.2 Independence
- 4.3 Transformations of random vectors
- 4.4 Multivariate Normal and Multinomial distributions
- 4.5 Sums of random variables
- 4.6 Mixtures
- 4.7 General concepto of random variable
- 4.8 Random sample
- 4.9 Order statistics
- 5. Properties of the expectation
- 5.1 Expectations of sums of random variables
- 5.2 Covariance
- 5.3 Conditional expectation
- 5.4 Conditional variance
- 5.5 Moment generating function
- 6. Limit Theorems
- 6.1 Markov and Chebishev inequalities
- 6.2 Weak Law of Large Numbers (convergence in probability)
- 6.3 Strong Law of Large Numbers (almost sure convergence)
- 6.5 Central Limit Theorem (convergence in distribution)

ASSESSMENT SYSTEM

Partial in-class exams: 50%

Final exam: 50%

% end-of-term-examination:	50
% of continuous assessment (assigments, laboratory, practicals):	50

BASIC BIBLIOGRAPHY

- Sheldon Ross A First Course in Probability, Pearson Prentice Hall, 2010

ADDITIONAL BIBLIOGRAPHY

- Charles M. Grinstead Grinstead and Snell's Introduction to Probability, University Press of Florida, 2009
- Dimitri P. Bertsekas, John N.Tsitsiklis Introduction to Probability, Athena Scientific, 2008

BASIC ELECTRONIC RESOURCES

- Sheldon Ross . A First Course in Probability: http://julio.staff.ipb.ac.id/files/2015/02/Ross_8th_ed_English.pdf