# uc3m Universidad Carlos III de Madrid

## Stochastic Processes

Academic Year: (2021 / 2022) Review date: 22-06-2021

Department assigned to the subject: Statistics Department Coordinating teacher: JIMENEZ RECAREDO, RAUL JOSE

Type: Compulsory ECTS Credits: 6.0

Year: 2 Semester: 1

## REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Elementary Statistical Theory I Elementary Statistical Theory II

#### **OBJECTIVES**

#### SPECIFIC SKILLS.

- 1. Knowing the theoretical foundations and the basic properties of stochastic processes.
- 2. Solve problems based on the studied stochastic models.
- 3. Simulating techniques for Markov Chains.

## **CUTTING SKILLS:**

- 1. Capacity for analysis and synthesis.
- 2. Problem solving.
- 3. Critical Thinking.

#### **DESCRIPTION OF CONTENTS: PROGRAMME**

- 1 Introduction
- 1.1 Random Variables
- 1.2 Random Vectors
- 1.3 Conditioned Expectation
- 1.4 Stochastic processes
- 2 Markov chains in discrete time
- 2.1 Definition
- 2.2 State classification
- 2.3 Stopping times
- 2.4 Limit Theorems
- 2.5 Limit and stationary distributions
- 3 Martingales in discrete time
- 3.1 Definition
- 3.2 Optional Stopping Theorem
- 3.3 Wald's Equation
- 3.4 Gambler's ruin problem
- 4 Continuous-time Stochastic Processes
- 4.1 Motivation
- 4.2 Various examples of processes with discrete state spaces.
- 4.3 Various examples of processes with continuous state spaces.
- 4.4 Applications

# LEARNING ACTIVITIES AND METHODOLOGY

Theory (4 ECTS). Lectures.

Practice (2 ECTS). Problem solving lessons.

#### ASSESSMENT SYSTEM

Final examination 40%. The remaining 60% will be grade through continuous evaluation, which will consist of tests, assignments and projects. All tests can contain application exercises, theoretical questions, and questions on computational practices. The student obtains a good grade in the

continuous assessment may exempt the final exam.

% end-of-term-examination:	40
% of continuous assessment (assigments, laboratory, practicals):	60

# **BASIC BIBLIOGRAPHY**

- R. Durrett Essentials of stochastic processes, Springer, 2012 (2nd ed.)
- S.M. Ross Stochastic Processes, John Wiley & Sons, inc., 1996 (2nd. ed.)

# BASIC ELECTRONIC RESOURCES

- R. Durrett . Essentials of Stochastic Processes: http://www.math.duke.edu/~rtd/EOSP/EOSP2E.pdf