

Academic Year: ( 2020 / 2021 )

Review date: 13-08-2020

Department assigned to the subject: Department of Mathematics

Coordinating teacher: DEAÑO CABRERA, ALFREDO

Type: Basic Core ECTS Credits : 6.0

Year : 2 Semester : 1

Branch of knowledge: Engineering and Architecture

**STUDENTS ARE EXPECTED TO HAVE COMPLETED**

Linear Algebra, Calculus I, Calculus II

**COMPETENCES AND SKILLS THAT WILL BE ACQUIRED AND LEARNING RESULTS.**

## A. Learning objectives (PO: a)

- A.1. To understand the concept of complex analyticity.
- A.2. To be able to compute the Laurent or Taylor series expansions associated to a function which is analytic in part of the complex plane, and to determine the region of convergence of such series.
- A.3. To acquire the basic concepts related to the elementary complex functions.
- A.4. To compute definite integrals by means of the residue calculus.
- A.5. To understand and solve first and second order linear homogeneous and non-homogeneous differential equations.
- A.6. To solve second order equations using power series methods.
- A.7. To recognise classical PDEs describing physical processes such as diffusion, wave propagation and electrostatics.
- A.8. To solve analytically, using the method of separation of variables, the heat and wave equations (in one space variable).

## B. Specific skills (PO: a)

- B.1. To understand the concept of complex differentiation and its practical applications.
- B.2. To be able to handle functions given in terms of series.
- B.3. To understand the concept of complex integration and its practical applications.
- B.4. To be able to solve first and second order linear homogeneous and non-homogeneous ODEs.
- B.5. To be able to solve second order ODEs using power series methods.
- B.5. To be able to model real-world problems using PDEs, and solve them using Fourier techniques.

## C. General skills (PO: a)

- C.1. To be able to think abstractly, and to use induction and deduction.
- C.2. To be able to communicate in oral and written forms using appropriately mathematical language.
- C.3. To be able to model a real situation using differential equation techniques.
- C.4. To be able to interpret a mathematical solution of a given problem, its accuracy, and its limitations.

**DESCRIPTION OF CONTENTS: PROGRAMME**

## 1. ORDINARY DIFFERENTIAL EQUATIONS.

First order equations. Second order linear equations. Power series solutions and special functions. Fourier series solutions of ODEs. The Laplace transform: Applications to differential equations.

## 2. COMPLEX ANALYSIS.

Analytic functions and singularities. Laurent series. Contour integration and Cauchy's integral formula. The residue theorem and its applications.

## 3. PARTIAL DIFFERENTIAL EQUATIONS.

Heat, wave, and Laplace equations. Fourier's method of separation of variables.

**LEARNING ACTIVITIES AND METHODOLOGY**

Lecture sessions: 3 credits (PO: a).

Problem sessions: 3 credits (PO: a).

## ASSESSMENT SYSTEM

We follow a continuous-assessment system plus a final exam:

- The continuous-assessment part consists in two exams with a 40% weight on the final mark (20% each). The exams will take place, approximately a week after the necessary lessons have been taught and it will be held in regular class hours, according to the current regulations.

- The final exam (contributing with weight 60% to the final mark) is compulsory, and will be held at the end of the semester. (PO: a.)

**% end-of-term-examination:** 60

**% of continuous assessment (assignments, laboratory, practicals...):** 40

## BASIC BIBLIOGRAPHY

- G. F. Simmons Differential equations with applications and historical notes , McGraw-Hill, 1991
- P. J. Hernando Clases de Ampliación de Matemáticas para Ingeniería, Revisión 3.2 - 2019.
- R. Haberman Elementary applied partial differential equations : with Fourier series and boundary value problems, Prentice Hall, 1998
- R. V. Churchill Complex variables and applications, McGraw-Hill, 1992