uc3m Universidad Carlos III de Madrid

Applied differential calculus

Academic Year: (2019 / 2020) Review date: 26/04/2019 18:45:25

Department assigned to the subject: Mathematics Department Coordinating teacher: CARRETERO CERRAJERO, MANUEL

Type: Basic Core ECTS Credits: 6.0

Year: 2 Semester: 2

Branch of knowledge: Engineering and Architecture

REQUIREMENTS (SUBJECTS THAT ARE ASSUMED TO BE KNOWN)

Calculus.

Linear Algebra.

OBJECTIVES

KNOWLEDGE (PO a - RA1.1):

- Solving linear differential equations and interpret results.
- Understand the concept of stability.
- Know how to plot slope fields.
- Know how to calculate Laplace transforms and how to use them to solve differential equations.
- Know how to solve systems of linear differential equations of first order.
- Understand the concept of Fourier series and using them to solve differential equations.
- Know how to use numerical methods to compute approximate solutions of first order non-linear systems of differential equations.

SPECIFIC ABILITIES (PO a - RA1.1):

- Increase the level of abstraction.
- To be able to solve practical problems using differential equations.

GENERAL ABILITIES (PO a - RA1.1):

- Ability to communicate orally and in writing correctly using signs and the language of mathematics.
- Ability to model a real situation described in words by differential equations.
- Ability to interpret the mathematical solution of a problem, their reliability and limitations.
- To be able to use mathematical software in specific situations.

DESCRIPTION OF CONTENTS: PROGRAMME

- 1.- First order differential equations:
 - a. Linear Equations.
 - b. Separable Equations.
 - c. Qualitative Techniques: Slope Fields. Equilibrium and Phase line. Bifurcations.
- 2.- Second Order Differential Equations.
 - a. Nonlinear and linear Equations.
 - b. Homogeneous Linear Equations.
 - c. Reduction of Order.
 - d. Euler-Cauchy Equations.
- 3.- Laplace transformations:
 - a. Definition.
 - b. Application to differential equations.
 - c. Convolution.
- 4.- Systems of differential equations:
 - a. Linear and Nonlinear Systems.
 - b. Vector representation.
 - c. Eigenvalues and linearization.
- 5. Fourier series and separation of variables:

- a. Basic results.
- b. Fourier Sine and Cosine Series.
- c. Convergence of Fourier series.
- d. Applications of Fourier series to Differential Equations.
- 6.- Numerical methods:
 - a. Euler method.
 - b. Runge-Kutta method.
 - c. Solution of boundary value problems.

LEARNING ACTIVITIES AND METHODOLOGY

Lectures sessions: 3.0 ECTS credits (PO:a - CGB1 - RA1).) Problem sessions: 3.0 ECTS credits (PO:a CGB1 - RA1).)

Office hours: each teacher offers a number of office hours according to the regulations of the Carlos III University. In particular, a minimum of one hour per group with time schedule compatible with the students.

ASSESSMENT SYSTEM

% end-of-term-examination/test: 60 % of continuous assessment (assignments, laboratory, practicals...): 40

We follow a continuous-assessment system (40%) plus a final exam (60%):

- The continuous-assessment part consists in a written examination contributing with weight 40% to the final mark. The mid-term examination will take place, approximately, at two thirds of the semester and it will be held in regular class hours, according to the current regulations.
- The final exam (contributing with weight 60% to the final mark) will be held at the end of the semester. (PO: a.)

BASIC BIBLIOGRAPHY

- Boyce, William E. Elementary differential equations and boundary value problems, John Wiley & Sons,.
- Simmons, George Finlay Differential equations with applications and historical notes 2nd ed., McGraw-Hill.
- Zill, Dennis G. Ecuaciones diferenciales con aplicaciones de modelado, International Thomson.

ADDITIONAL BIBLIOGRAPHY

- Gockenbach, Mark S. Partial differential equations: analytical and numerical methods, SIAM.
- Haberman, Richard Elementary applied partial differential equations with Fourier series and boundary value problems 3rd ed, Prentice Hall.
- Kiseliov, Aleksandr I. Problemas de ecuaciones diferenciales ordinarias , Mir.
- Weinberger, Hans F. A first course in partial differential equations with complex variables and transform methods, Dover.