# uc3m Universidad Carlos III de Madrid

#### Calculus I

Academic Year: (2018 / 2019) Review date: 16-04-2018

Department assigned to the subject: Mathematics Department Coordinating teacher: LOPEZ LAGOMASINO, GUILLERMO

Type: Basic Core ECTS Credits: 6.0

Year: 1 Semester: 1

Branch of knowledge: Engineering and Architecture

#### **OBJECTIVES**

- a. To understand the concept of real number and its implications, mainly the concept of limit.
- b. To understand and manipulate series of real numbers.
- c. To identify functions, their dependence on variables and their basic properties (monotony, parity, continuity, differentiability).
- d. To master the basic operations of Calculus: limits, derivatives, integrals and Taylor expansions.
- e. To interpret the derivative as rate of variation of a function, and the integral as an area.
- f. To understand the Taylor polynomial as the best polynomial local approximation for a sufficiently smooth function, and to apply that approximation to simple cases.
- g. To be able to graph simple functions.
- h. To be able to solve simple optimization problems.

# **DESCRIPTION OF CONTENTS: PROGRAMME**

Part I: Real Numbers and Functions

Chapter 1: The Real Line

- 1.1 Ordered Fields
- 1.2 Number Systems
- 1.3 Absolute value, bounds, and intervals

# Chapter 4: Real Functions

- 2.1 Definition and basic concepts
- 2.2 Elementary functions
- 2.3 Operations with functions

# Part II: Sequences and Series

### Chapter 3: Sequences

- 3.1 Sequences of real numbers
- 3.2 Limit of a sequence
- 3.3 Number e
- 3.4 Indeterminacies
- 3.5 Asymptotic comparison of sequences

#### Chapter 4: Series

- 4.1 Series of real numbers
- 4.2 Series of nonnegative terms
- 4.3 Alternating series
- 4.4 Telescopic series

Part III: Differential Calculus

#### Chapter 5: Limit of a Function

- 5.1 Concept and definition
- 5.2 Algebraic properties
- 5.3 Asymptotic comparison of functions

#### Chapter 6: Continuity

- 6.1 Definition, properties, and continuity of elementary functions
- 6.2 Discontinuities
- 6.3 Continuous functions in closed intervals

#### Chapter 7: Derivatives

- 7.1 Concept and definition
- 7.2 Algebraic properties
- 7.3 Derivatives and local behaviour

# Chapter 8: Taylor expansions

- 8.1 Asymptotic comparison of functions
- 8.2 Taylor¿s polynomial
- 8.3 Calculating limits
- 8.4 Remainder and Taylor is theorem
- 8.5 Taylor series
- 8.6 Numerical approximations
- 8.7 Local behaviour of functions
- 8.8 Function graphing

# Part IV: Integral Calculus

## Chapter 9: Primitives

- 9.1 Integration by parts
- 9.2 Primitives of rational functions
- 9.3 Change of variable

#### Chapter 10: Fundamental Theorem of Calculus

- 10.1 Riemann¿s integral
- 10.2 Properties of the integral
- 10.3 Riemann¿s sums
- 10.4 Fundamental theorem of calculus

#### Chapter 11: Geometric Applications of Integrals

- 11.1 Area of flat figures
- 11.2 Area of flat figures in polar coordinates
- 11.3 Volumes
- 11.4 Length of curves

#### LEARNING ACTIVITIES AND METHODOLOGY

The methodology will be the usual one for classes in the classroom, writing on the blackboard, with the occasional help of some resources on-line to illustrate some graphic or computational aspects of the course. Also, the classroom notes will be uploaded in Aula Global at the end of each chapter, along with the problem sheets that will be solved and discussed in the small groups.

#### ASSESSMENT SYSTEM

The final grade will be assigned through the students' performance in two kinds of tests: three in-class tests, with a weight of 40% in the final grade, together with a final exam, amounting to 60% of the final grade. Failing to attend any of the in-class tests implies obtaining 0 points in that test. The weights above, as well as the points obtained in the in-class tests, will be kept for those students who have to take the extraordinary exam.

% end-of-term-examination: 60 % of continuous assessment (assignments, laboratory, practicals...): 40

#### **BASIC BIBLIOGRAPHY**

- H. Anton, I.C. Bevis & S. Davis Calculus: Early Transcendentals Single Variable, Wiley, 2008
- J. Stewart Single variable calculus: early transcendentals, Brooks-Cole, 1999

- R. Larson, R.P. Hostetler & B.H. Edwards Calculus, Brooks-Cole, 2005
- S.L. Salas, G.J. Etgen & E. Hille Calculus: One and Several Variables, Wiley, 2006

# ADDITIONAL BIBLIOGRAPHY

- T.M. Apostol Calculus vol. 1, Wiley, 1991